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# Modules of Elasticity and Thermal Expansion Coefficient of ITO Film

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# Modulus of Elasticity and Thermal Expansion Coefficient of ITO Film

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## Introduction

The purpose of this experiment was to determine the modulus of elasticity ( $E$ ) and thermal expansion coefficient ( $\alpha$ ) of RF sputtered Indium Tin Oxide (ITO) as a function of temperature ( $T$ ), and to collect ITO film stress data.

In order to accomplish that goal, the Toho FLX-2320-S thin film stress measurement machine was used to collect both single stress and stress-temperature data for ITO coated fused silica and sapphire substrates. The stress measurement function of the FLX-2320-S cannot be used to calculate the elastic modulus of the film because the Stoney formula (shown below) incorporates the elastic modulus of the substrate, rather than of the film itself.

$$\sigma_f = \frac{E_s}{1-\nu_s} \left( \frac{h_s^2 k}{6h_f} \right) \quad (1)$$

where  $\sigma_f$  is the film stress,  $E_s$  is the elastic modulus of the substrate,  $\nu_s$  is Poisson's ratio of the substrate,  $h_{s,f}$  is the thickness of the substrate and film, and  $k$  is the curvature of the wafer. However, the thin film stress measurement tool has an elastic and expansion coefficient function that uses film stress as a function of temperature of two different substrates coated with the same film to calculate and plot the linear thermal expansion coefficient with respect to time, as well as the biaxial modulus of the film. In order to accomplish this, the FLX-2320 substitutes the data collected for each of the two substrates into separate Equation 2's, and then solves the two resulting equations for the film's biaxial modulus ( $\frac{E}{1-\nu}$ ) and coefficient of thermal expansion ( $\alpha_f$ ).

$$\frac{d\sigma(f)}{dT} = \left( \frac{E}{1-\nu} \right)_f (\alpha_s - \alpha_f) \quad (2)$$

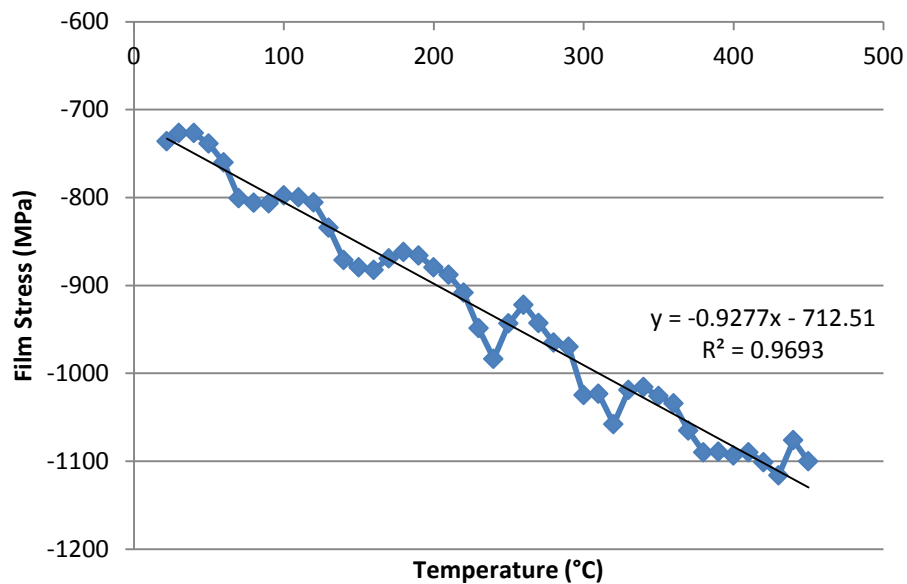
## Experimental Results and Discussion

Before coating the fused silica and sapphire substrates with the ITO film, their thickness was measured and blank measurements using the FLX-2320-S were taken, which determined the curvature of the substrate surface. It was found that the fused silica sapphire substrates had thicknesses of approximately 525  $\mu\text{m}$  and 435  $\mu\text{m}$ , respectively. The radius of curvature of the fused silica was -4.97 m, and it was 2.09 m for the sapphire. The samples were then coated with the ITO film at the Vacuum Process Lab (VPL). Both of the samples were coated in the same

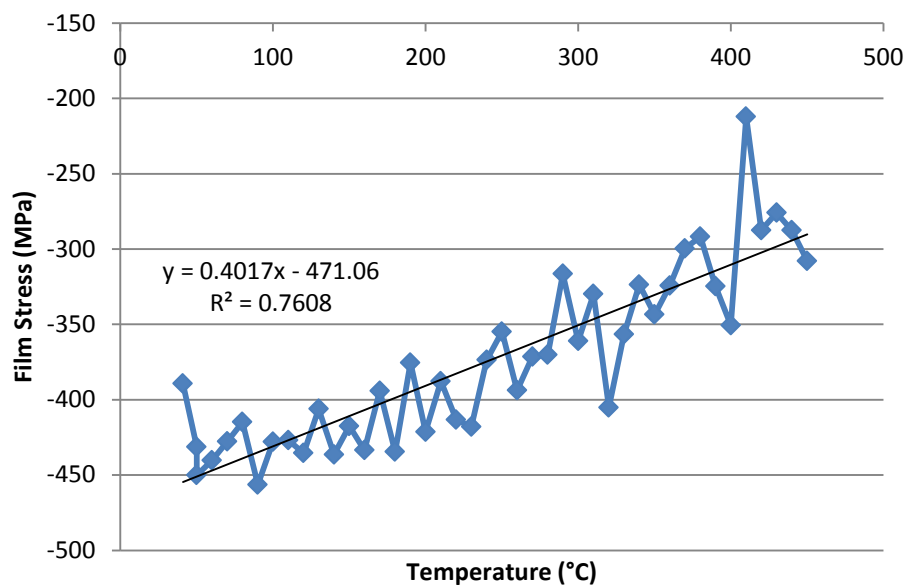
deposition run, and the average thickness of the ITO film was determined to be 2,157 Ångströms using a witness strip.

Once coated, it was determined using the confocal that the samples were in pristine condition, with no obvious signs of damage or debris. The four point probe was then used to measure the electrical resistivity of the ITO film, which was found to be between 51 and 92 ohms per square for both substrates. The FLX-2320 was then used to collect stress data as a function of temperature for each of the samples. The substrates were heated from room temperature to 350 degrees Celsius in approximately 30 minutes, and then they were immediately allowed to cool. Throughout the heating, stress measurements were collected. This initial annealing run caused the electrical resistivity of the ITO film to increase significantly to values between 281 and 994 ohms per square. It was determined by confocal inspection that the film was not completely annealed on either substrate, which was causing the increase in electrical resistivity. The two substrates were again ramped to 350 degrees Celsius in 30 minutes; however, they were held at that temperature for 20 minutes. Following this run, the electrical resistivity of the film decreased to between 185 and 484 ohms per square, and it was determined using the confocal that the films were completely annealed. In the final temperature-dependent stress experiment, the samples were raised from room temperature to 450 degrees Celsius in 1 hour and 43 minutes, which equates to a ramp of 4.2 degrees Celsius per minute. The electrical resistivity of the ITO film after this final run was approximately 100 ohms per square for the fused silica substrate and 250 ohms per square for the sapphire substrate. Figures 1 and 2 below show the film stress for each sample as a function of temperature for the final FLX-2320 run.

**Figure 1: Temperature-Dependent Stress (Fused Silica w/ITO Film)**

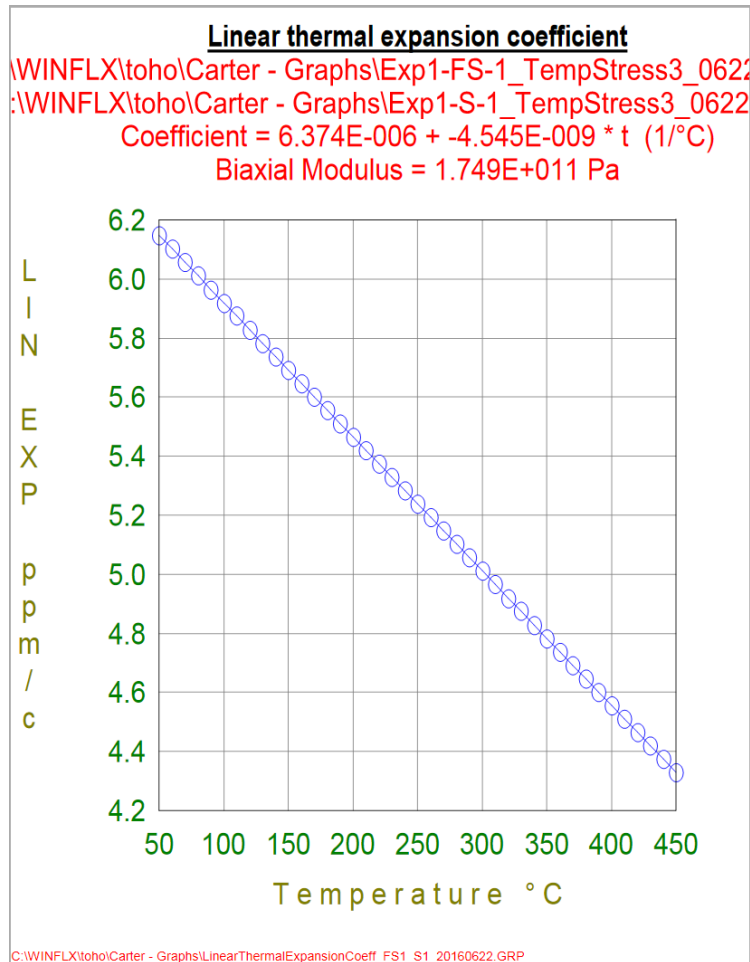


**Figure 2: Temperature-Dependent Stress (Sapphire w/ITO Film)**



## Data Analysis

Using Equation 2, the elastic and expansion coefficient function in the thin film stress measurement machine graphs the film's linear coefficient of thermal expansion (CTE) with respect to temperature and calculates the CTE equation and the average biaxial modulus of the film.



**Figure 3: Linear Thermal Expansion Coefficient of ITO**

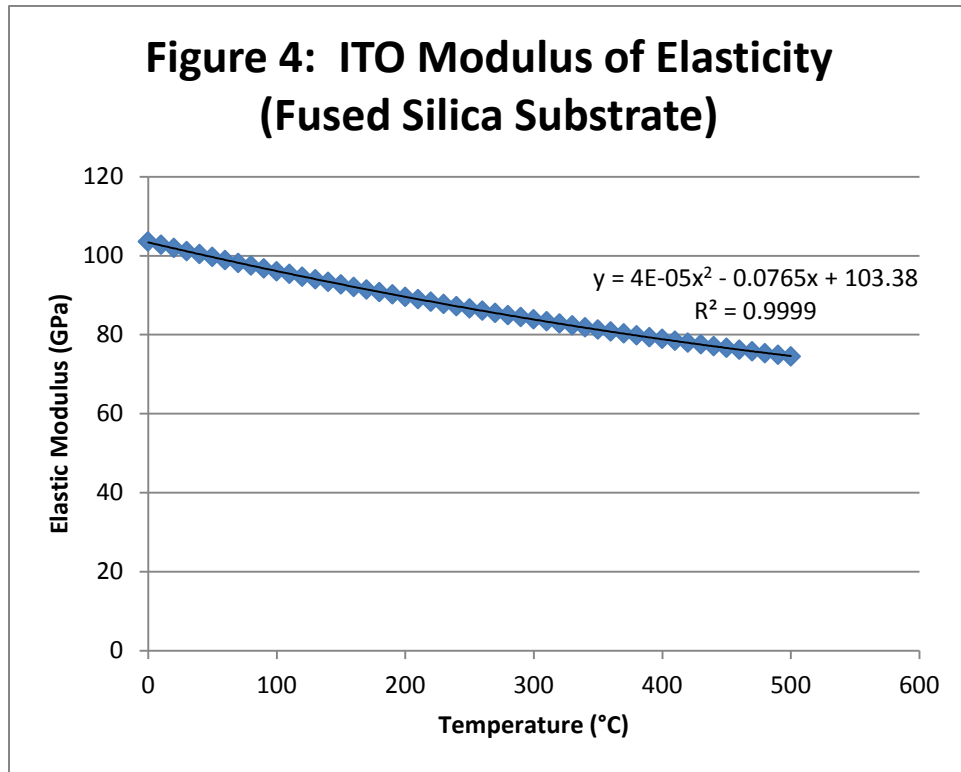
Using the published ITO Poisson ratio of 0.35, it was determined that the average modulus of elasticity of the film over the range of temperatures at which film stress was measured is 113.7 GPa, which is very near the published value of 116 GPa. The first step in calculating the ITO's elastic modulus as a function of temperature was to find an equation that describes the relationship between the film stress and temperature, which was accomplished using a trend line in Excel and can be seen in Figures 1 and 2. This equation was then differentiated and substituted, along with the equation of the ITO's linear CTE, the published substrate CTE, and the published ITO Poisson ratio, into Equation 2. The resulting equation was

then solved for the ITO film's elastic modulus (E). Equations 3 and 4 show this equation for the fused silica and sapphire substrates, respectively.

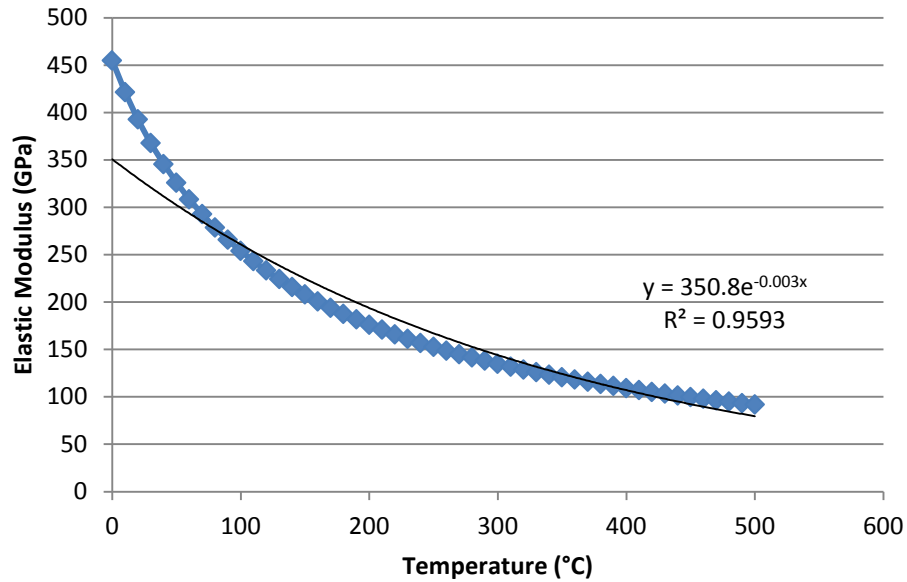
$$E = \frac{-0.9277 \text{ MPa}}{(0.55*10^{-6}-6.374*10^{-6}-4.545*10^{-9}*T)_{\text{°C}}^{\frac{1}{C}}} (1 - 0.35) \quad (3)$$

$$E = \frac{0.4017 \text{ MPa}}{(5.8*10^{-6}-6.374*10^{-6}-4.545*10^{-9}*T)_{\text{°C}}^{\frac{1}{C}}} (1 - 0.35) \quad (4)$$

Finally, the ITO's elastic modulus was calculated for a range of temperatures between 0 and 500 degrees Celsius using Equations 3 and 4 and graphed (Figures 4 and 5).



**Figure 5: ITO Modulus of Elasticity  
(Sapphire Substrate)**



## Conclusion

The average modulus of elasticity of ITO based on the calculations performed using Equations 3 and 4 is 136.62 GPa. Based on the published elastic modulus of ITO film, the calculated value has an error of 17.78%, and the 113.7 GPa value provided by the thin film stress measurement machine only has a 1.98% error. In order to improve the analysis of the data, the stress versus temperature graphs could be smoothed, which would provide for a better trend line and ultimately more accurate elastic modulus calculations.



## Appendix A

Summary of Parameters Used in Analysis:

	<u>Fused Silica</u>	<u>Sapphire</u>	<u>ITO Film</u>
Sample ID	Exp1-FS-1	Exp1-S-1	N/A
CTE	$0.55 \times 10^{-6} \text{ 1/}^\circ\text{C}$	$5.8 \times 10^{-6} \text{ 1/}^\circ\text{C}$	$6.374 \times 10^{-6} - 4.545 \times 10^{-9} \text{ T}$ $1/^\circ\text{C}$
Poisson Ratio	0.17	0.25	0.35
Published Elastic Modulus	73 GPa	345 GPa	116 GPa
FLX Calculated Elastic Modulus	N/A	N/A	113.7 GPa
Thickness	525 $\mu\text{m}$	435 $\mu\text{m}$	215.7 nm

1<sup>st</sup> FLX Temperature Cycle of Exp1-FS-1 and Diamond Substrate (6-20-16)

Start Temp: 45°C

End Temp: 350°C

Start Time: 1340

End Time: 1415

ID: FS1

Comment: FS1\_Temp

Film Thickness: 2157 Å

Orientation: 0°

Laser: 670 nm

Recipe:

Temp (°C)	Time (min.)	Measurements	Ramp (°C/min.)
50	4	5	1.3
100	4	10	12.5
150	4	10	12.5
200	4	10	12.5
250	4	10	12.5
300	4	10	12.5
350	4	10	12.5

1<sup>st</sup> FLX Temperature Cycle of Exp1-S-1 (6-20-16)

Start Temp: 22°C

End Temp: 352°C

Start Time: 1207

End Time: 1237

ID: S1

Comment: S1\_Temp

Film Thickness: 2157 Å

Orientation: 0°

Laser: 780 nm

Recipe:

Temp (°C)	Time (min.)	Measurements	Ramp (°C/min.)
50	4	5	7.3
100	4	10	12.5
150	4	10	12.5
200	4	10	12.5
250	4	10	12.5
300	4	10	12.5
350	4	10	12.5

2<sup>nd</sup> FLX Temperature Cycle of Exp1-FS-1 and Diamond Substrate (6-21-16)

Start Temp: 24°C

End Temp: 350°C

Start Time: 0953

End Time: 1043

ID: FS1

Comment: FS1\_Temp2

Film Thickness: 2157 Å

Orientation: 0°

Laser: 670 nm

Recipe:

Temp (°C)	Time (min.)	Measurements	Ramp (°C/min.)
50	4	5	6.5
100	4	10	12.5
150	4	10	12.5
200	4	10	12.5
250	4	10	12.5
300	4	10	12.5
350	4	10	12.5
350	20	5	0.0

2<sup>nd</sup> FLX Temperature Cycle of Exp1-S-1 (6-21-16)

Start Temp: 40°C

End Temp: 350°C

Start Time: 1155

End Time: 1245

ID: S1

Comment: S1\_Temp2

Film Thickness: 2157 Å

Orientation: 0°

Laser: 670 nm

Recipe:

Temp (°C)	Time (min.)	Measurements	Ramp (°C/min.)
50	4	5	2.5
100	4	10	12.5
150	4	10	12.5
200	4	10	12.5
250	4	10	12.5
300	4	10	12.5
350	4	10	12.5
350	20	5	0.0

3<sup>rd</sup> FLX Temperature Cycle of Exp1-FS-1 (6-22-16)

Start Temp: 22°C

End Temp: 450°C

Start Time: 1105

End Time: 1250

ID: FS1

Comment: FS1\_Temp3

Film Thickness: 2157 Å

Orientation: 0°

Laser: 670 nm

Recipe:

Temp (°C)	Time (min.)	Measurements	Ramp (°C/min.)
50	7	10	4.0
100	12	10	4.2
150	12	10	4.2
200	12	10	4.2
250	12	10	4.2
300	12	10	4.2
350	12	10	4.2
400	12	10	4.2
450	12	10	4.2

3<sup>rd</sup> FLX Temperature Cycle of Exp1-S-1 (6-22-16)

Start Temp: 41°C

End Temp: 450°C

Start Time: 1411

End Time: 1557

ID: S1

Comment: S1\_Temp3

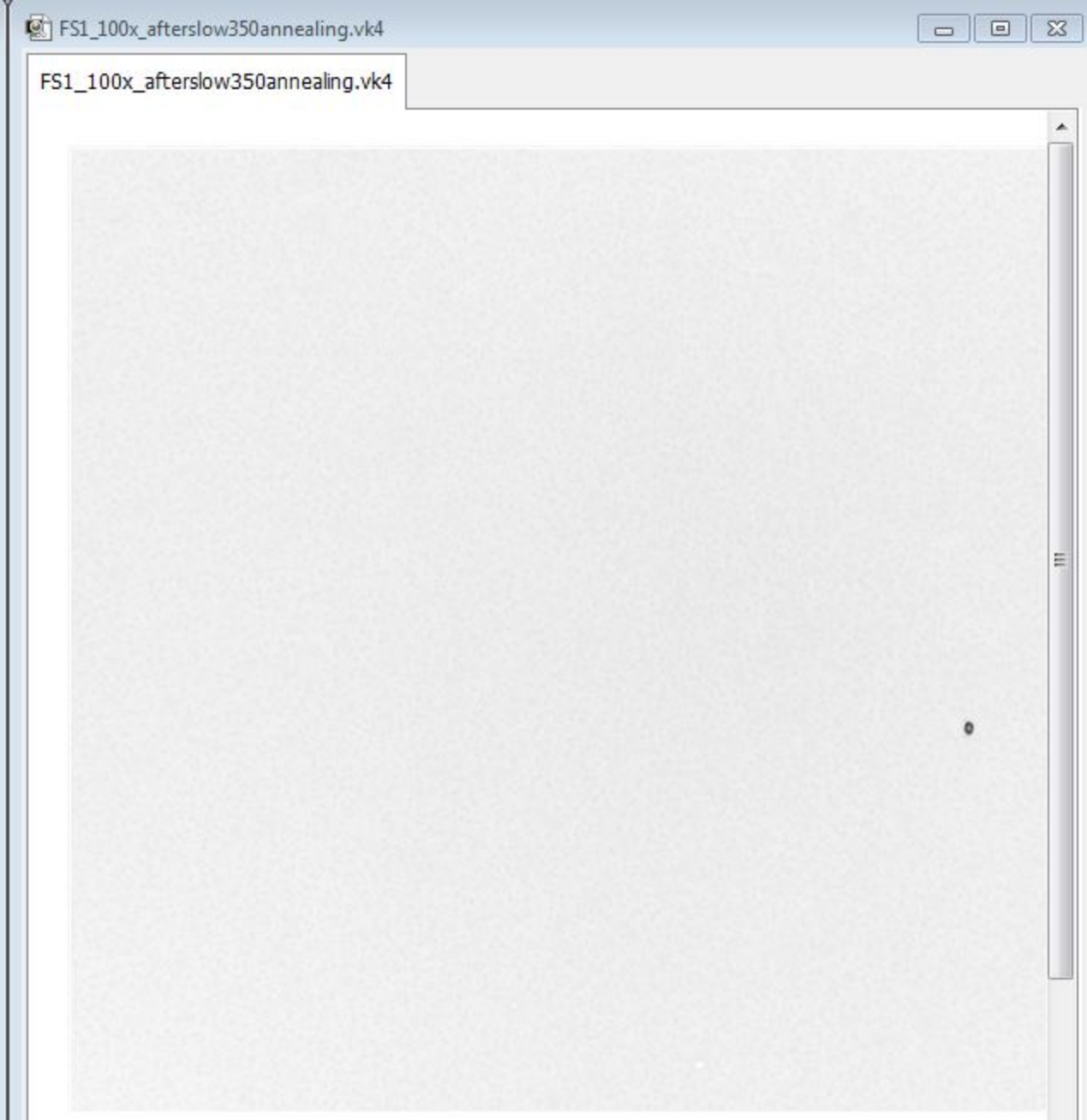
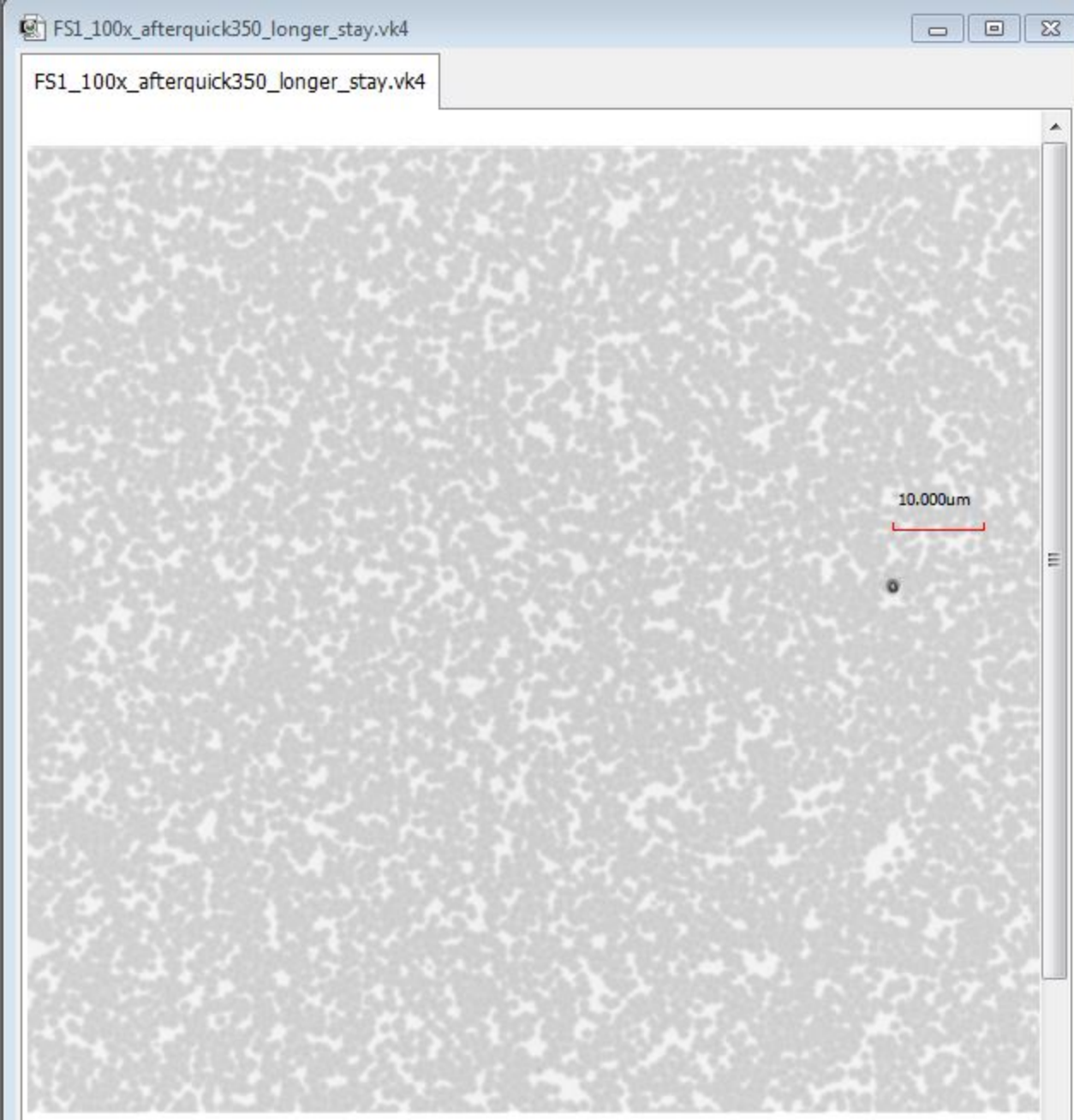
Film Thickness: 2157 Å

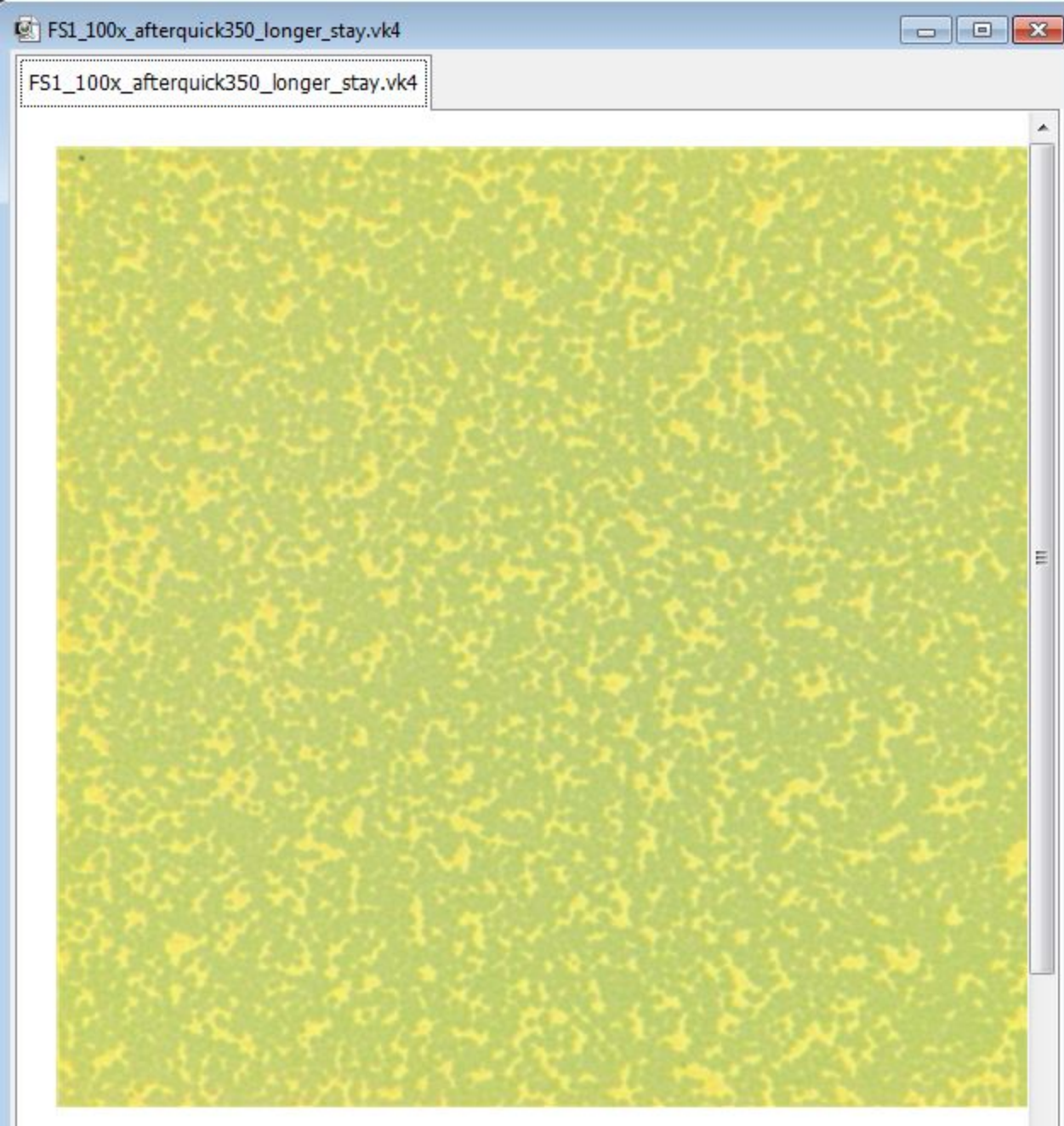
Orientation: 0°

Laser: 670 nm

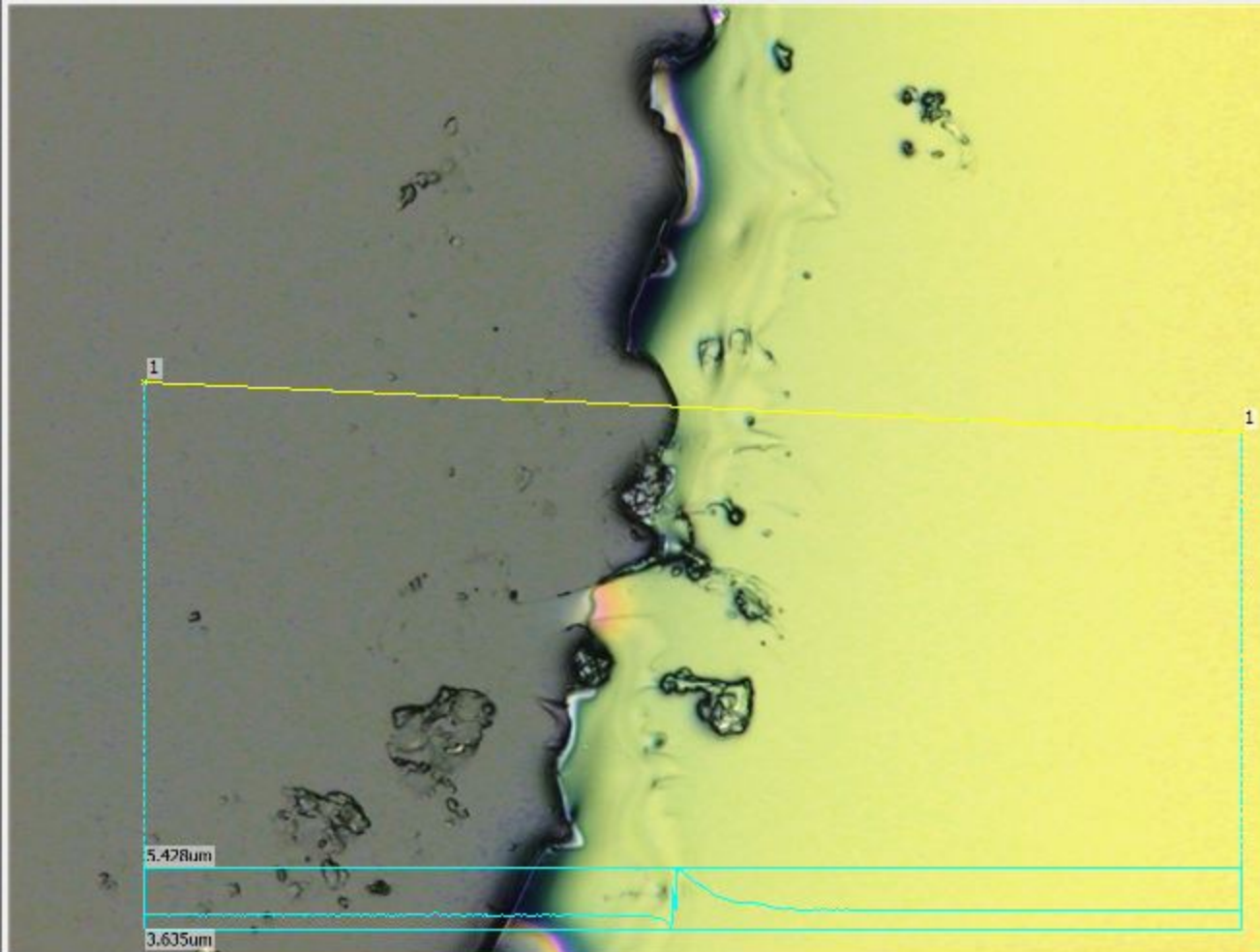
Recipe:

Temp (°C)	Time (min.)	Measurements	Ramp (°C/min.)
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100	12	10	4.2
150	12	10	4.2
200	12	10	4.2
250	12	10	4.2
300	12	10	4.2
350	12	10	4.2
400	12	10	4.2
450	12	10	4.2









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Display image Laser+Optical

Magnification Auto

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Vert.

Horz.

Pivot

Perp.

Para.

3pt. circ.

2pt. circ.

Ellipse

Multi line

Fixed len.

☐ Average profile

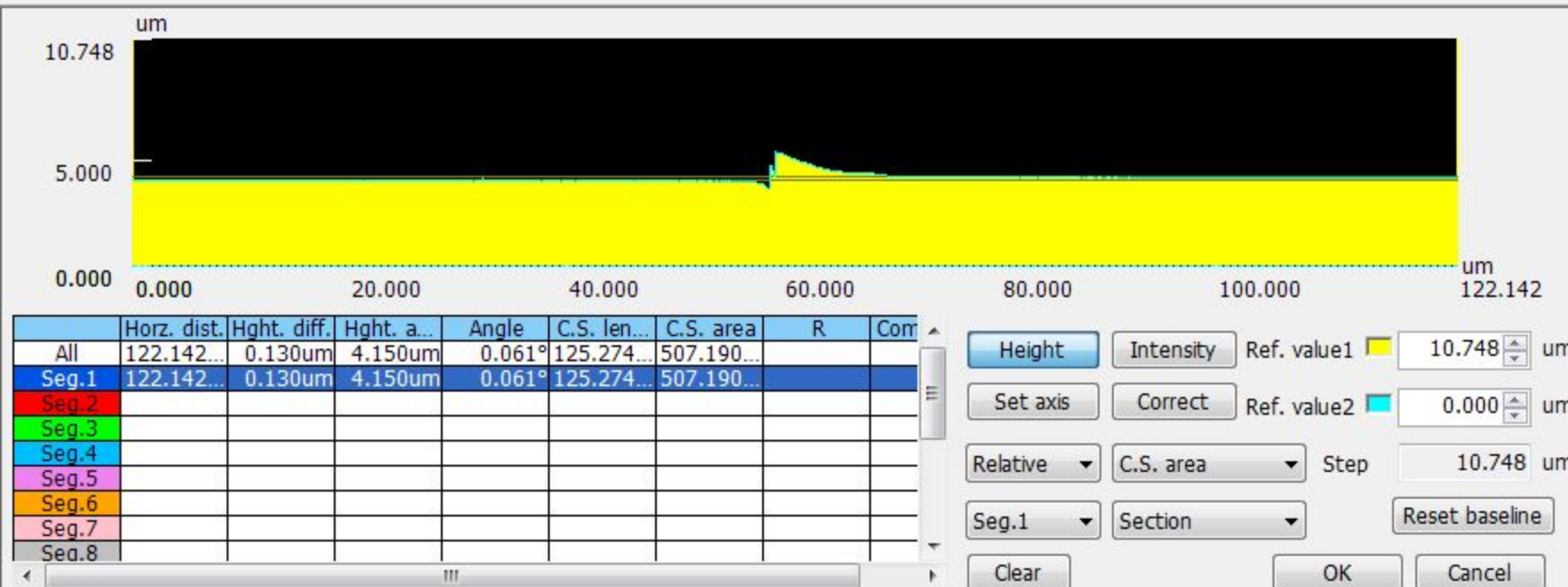
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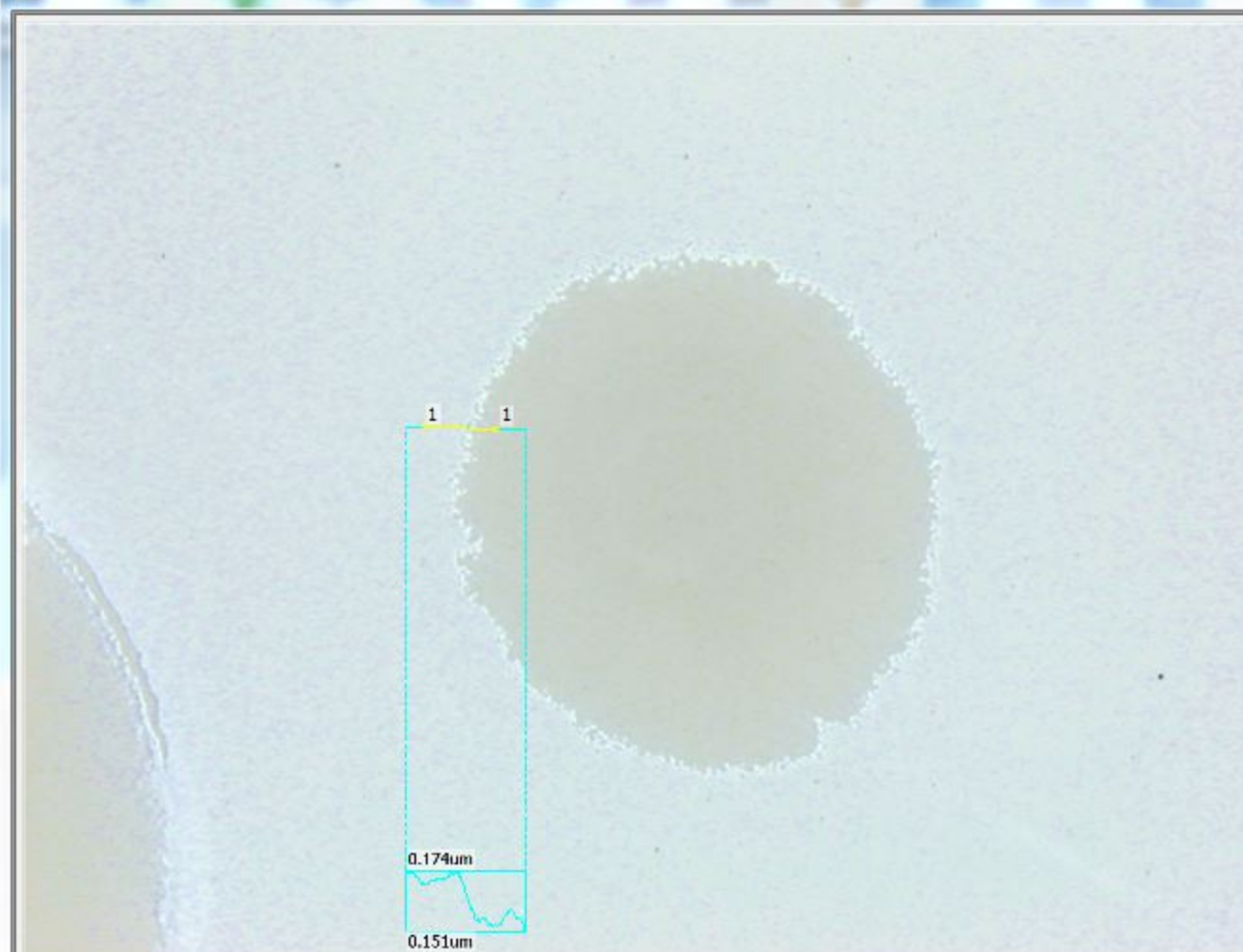
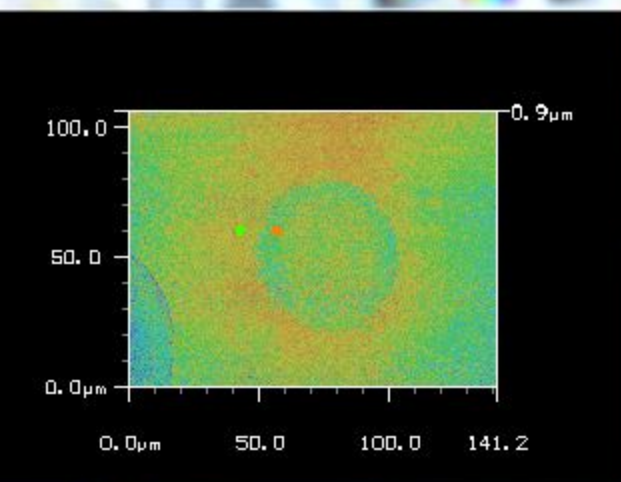
Line color

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Add line Delete line

Measurement line history





3DViewer 3D settings

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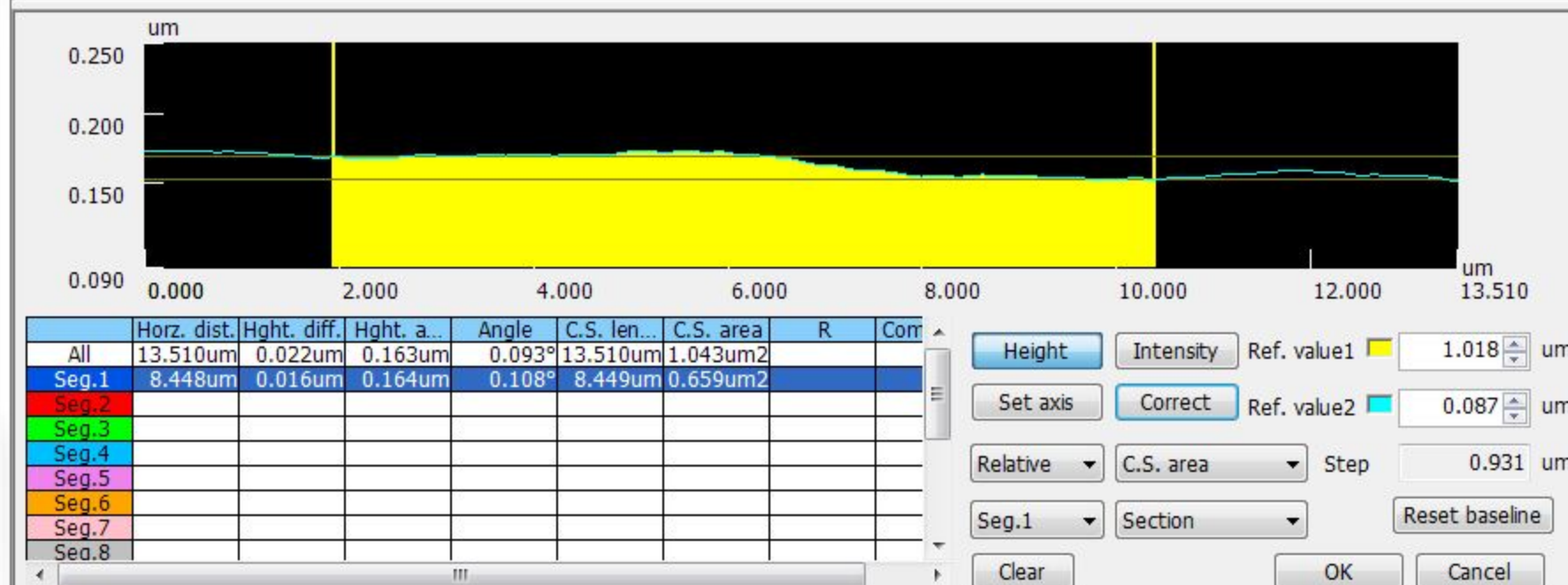
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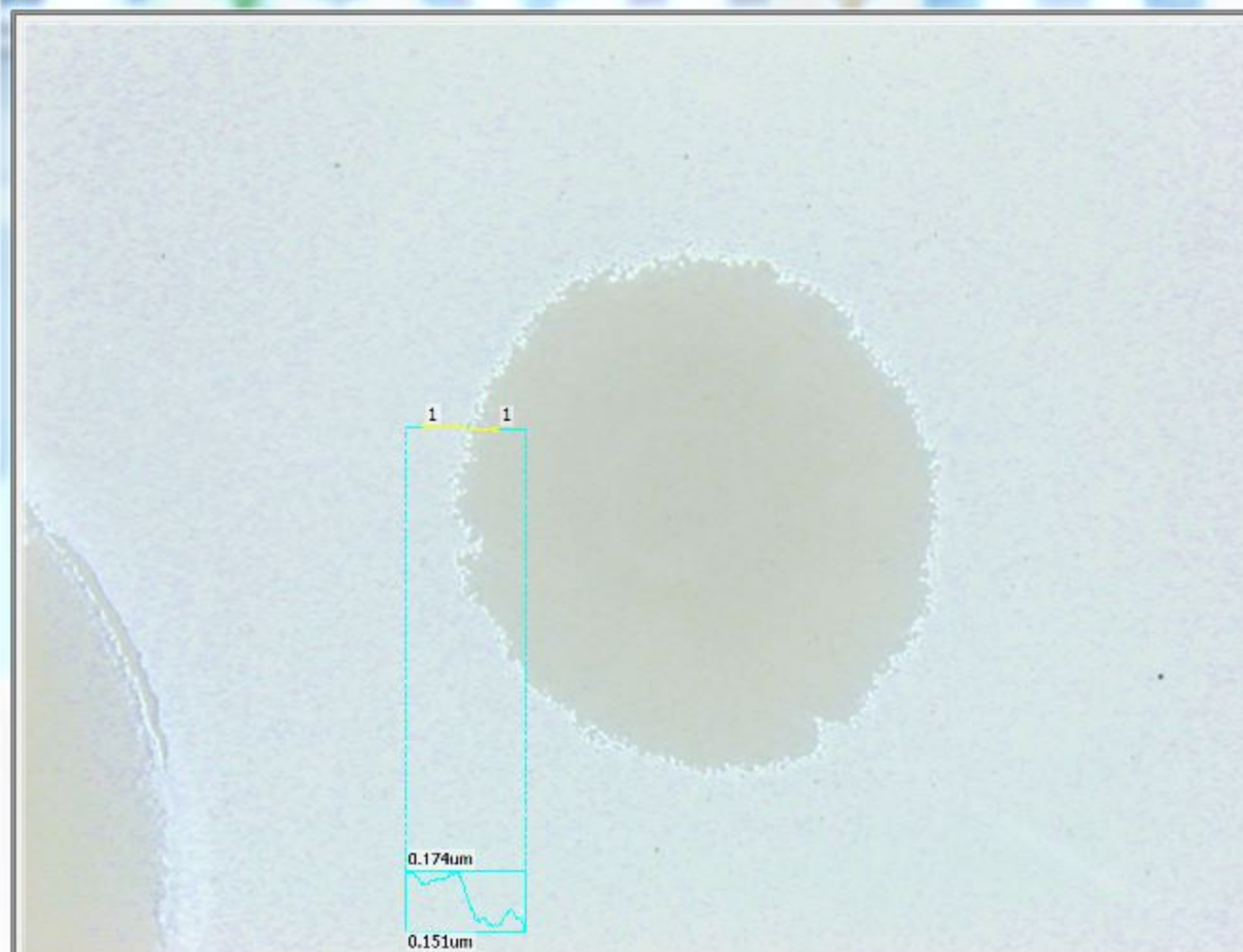
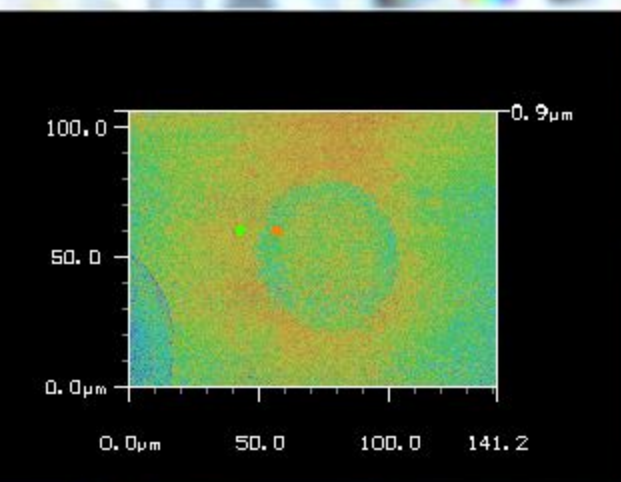


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Height =0.155um

Intensity =60053





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Display image Laser+Optical

Magnification Auto

Set 2pt. Vert. Horz.

Pivot Perp. Para.

3pt. circ. 2pt. circ. Ellipse

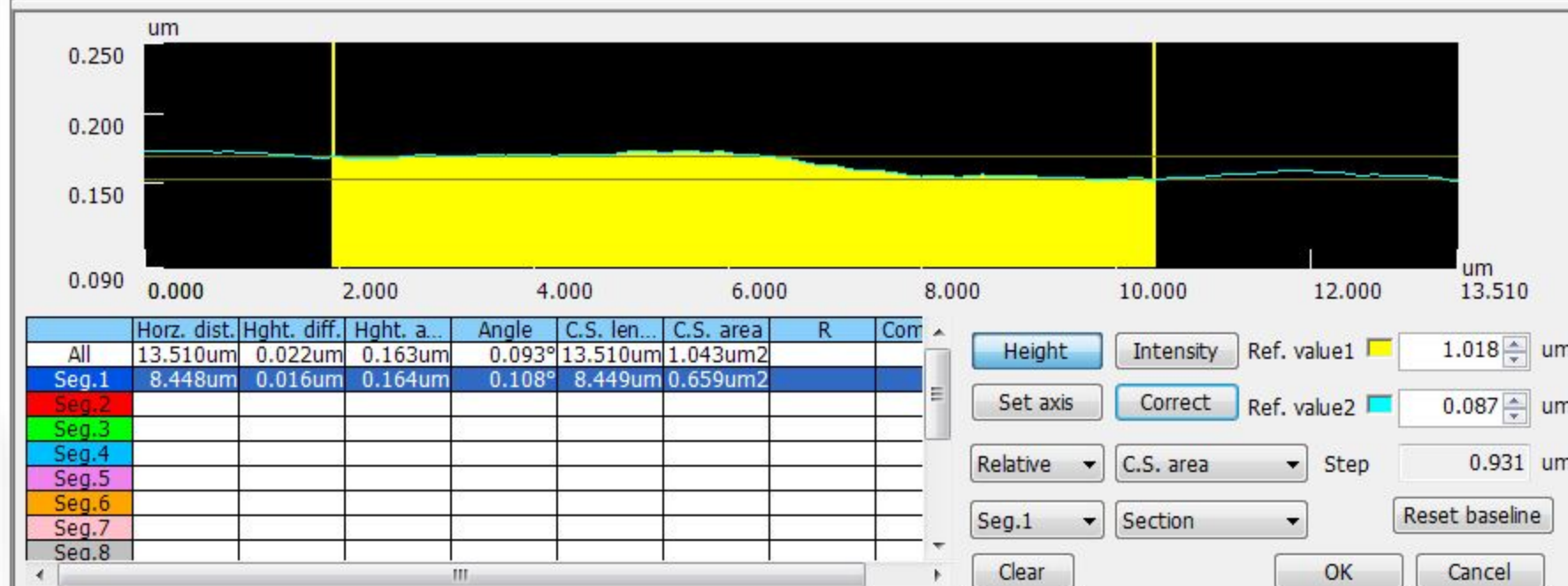
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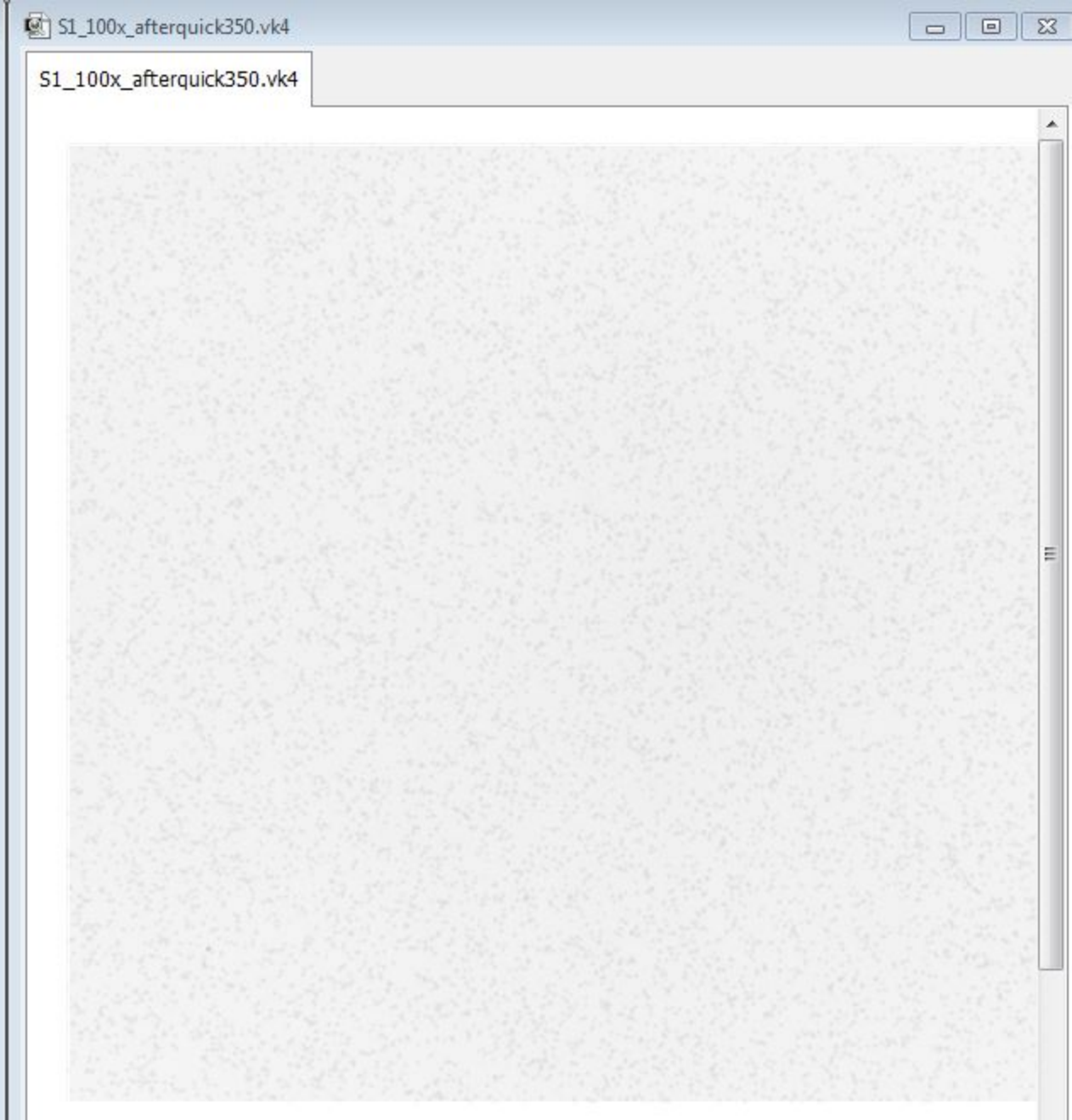
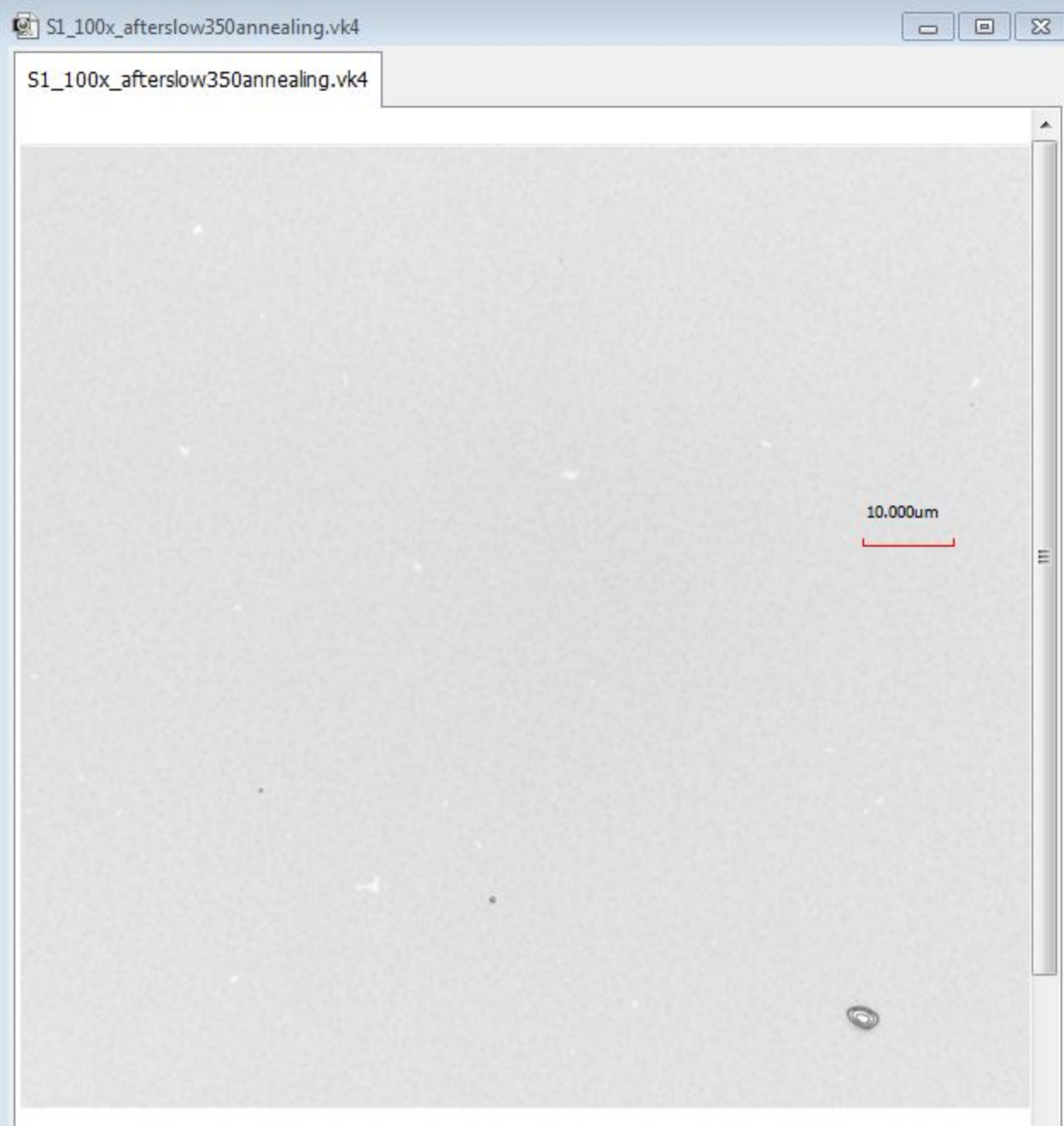
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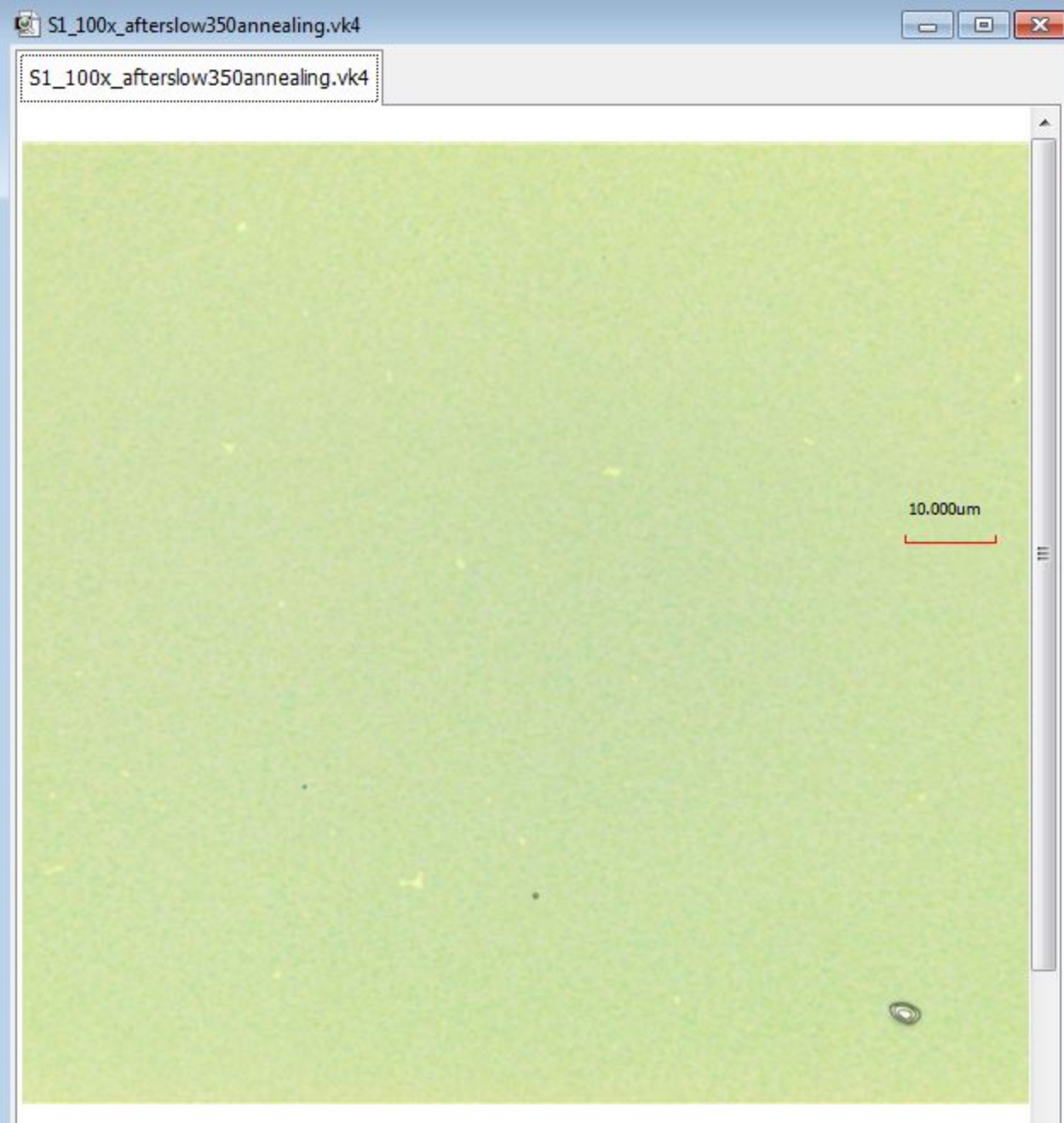
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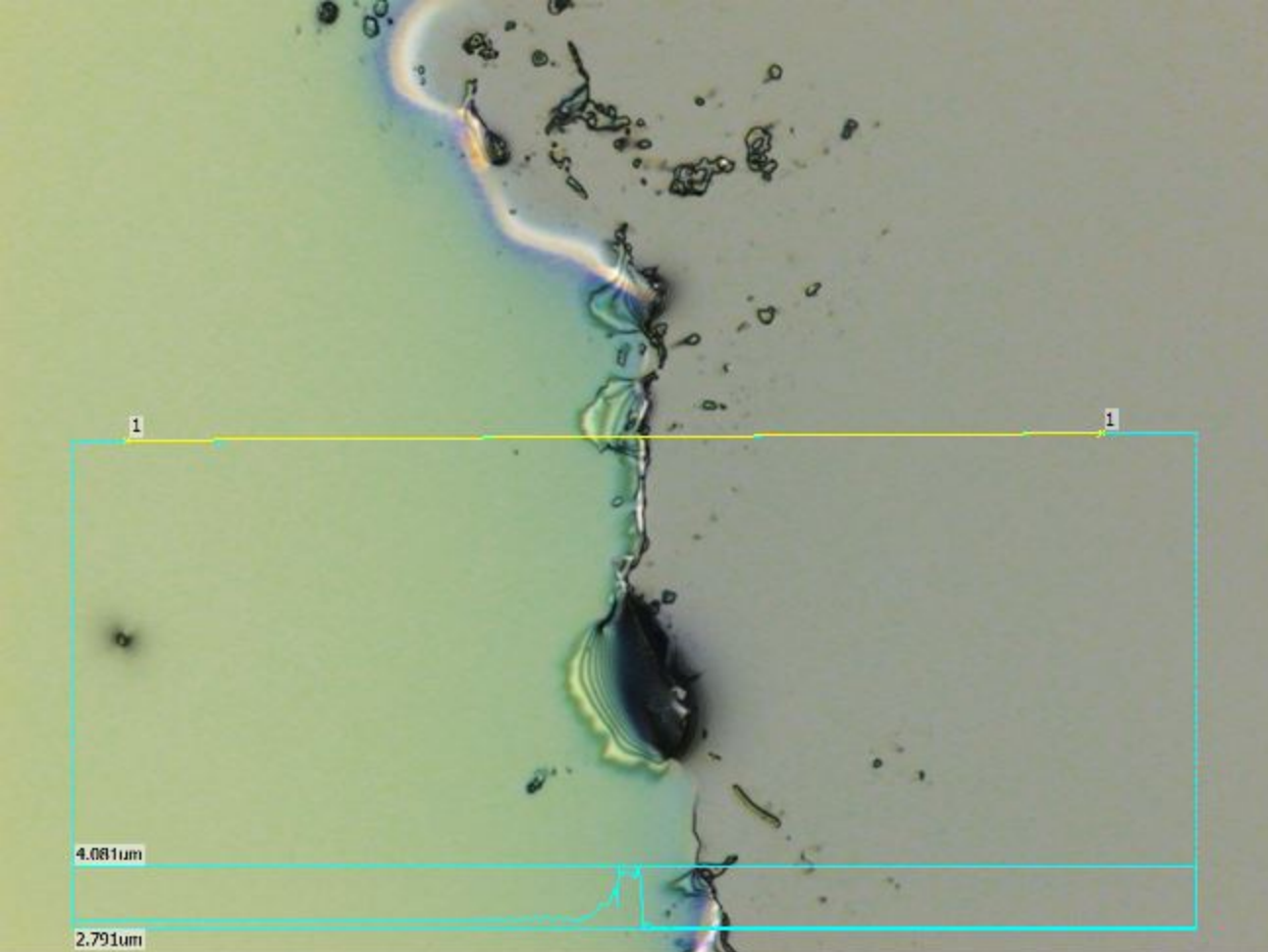
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3DViewer 3D settings

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Pivot Perp. Para.

3pt. circ. 2pt. circ. Ellipse

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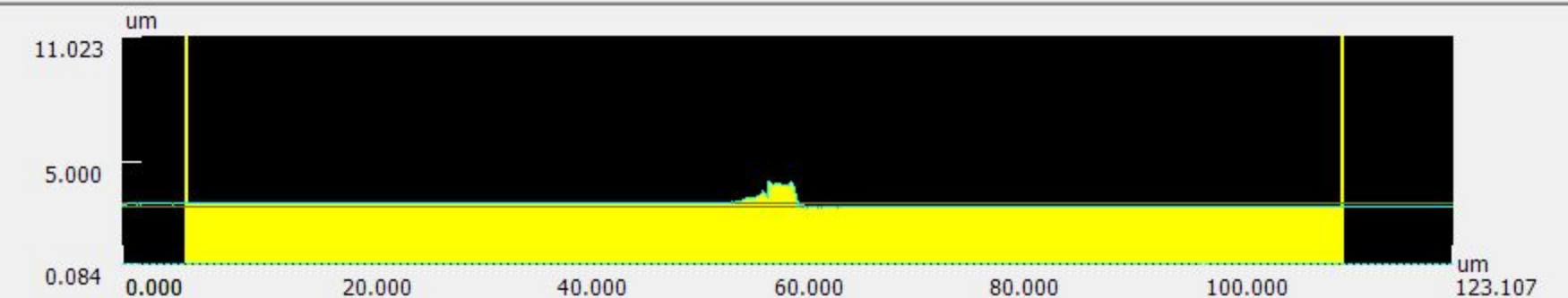
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Line color

Select line Profile1

Add line Delete line

Measurement line history



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All	123.107...	0.143um	2.928um	0.067°	125.631...	350.337...		
Seg.1	107.014...	0.159um	2.937um	0.085°	109.478...	305.364...		
Seg.2								
Seg.3								
Seg.4								
Seg.5								
Seg.6								
Seg.7								
Seg.8								

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Set axis Correct Ref. value2 0.084 um

Relative C.S. area Step 10.939 um

Seg.1 Section Reset baseline

Clear OK Cancel

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